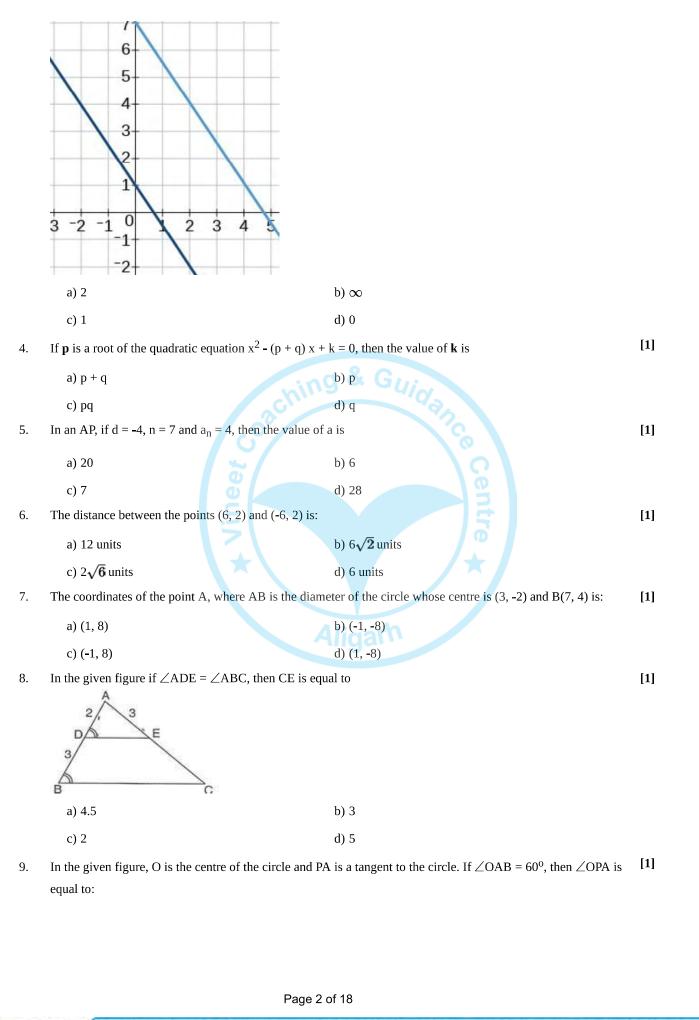


Class X Session 2024-25 Subject - Mathematics (Basic) Sample Question Paper - 5

	owed: 3 hours	Μ	aximum Marks: 80
eneral	Instructions:		
	1. This Question Paper has 5 Sections A, B,	C, D and E.	
	2. Section A has 20 MCQs carrying 1 mark	each	
	3. Section B has 5 questions carrying 02 ma	rks each.	
	4. Section C has 6 questions carrying 03 ma	rks each.	
	5. Section D has 4 questions carrying 05 ma	rks each.	
	6. Section E has 3 case based integrated unit	s of assessment carrying 04 marks each.	
	7. All Questions are compulsory. However,	an internal choice in 2 Qs of 5 marks, 2 Qs of 3 marks	s and 2 Questions of
	2 marks has been provided. An internal cl	hoice has been provided in the 2 marks questions of S	Section E
	8. Draw neat figures wherever required. Tak	e $\pi = \frac{22}{7}$ wherever required if not stated.	
		Section A	
1.	The least positive integer divisible by 20 and	Section A 1 24 is	[1]
	a) 480	b) 240	
	c) 360	d) 120	
2.	If the diagram in Fig. shows the graph of the	polynomial $f(x) = ax^2 + bx + c$, then	[1]
	$\left(\frac{-b}{2a},\frac{-D}{4a}\right)$ \uparrow y	Aligam	
	\frown		
	$\left \begin{array}{c} x' \\ x' \\ \end{array} \right = ax^2 + bx + c$		
	f(x) = ax + bx + c		
	a) a < 0, b < 0 and c < 0	b) a < 0, b > 0 and c > 0	
	c) a < 0, b < 0 and c > 0	d) a < 0, b > 0 and c < 0	
	The number of solutions for two linear equat		

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	A 60° B P		
	a) 300	b) ₂₀ °	
	c) ₁₅ 0	d) ₆₀ °	
10.	A tangent to a circle is a line that touches the circle at		[1]
	a) three points	b) one point only	
	c) infinite number of points	d) two points	
11.	If $2x = \sec A$ and $\frac{2}{x} = \tan A$ then $2\left(x^2 - \frac{1}{x^2}\right) = ?$		[1]
	a) $\frac{1}{2}$	b) $\frac{1}{4}$	
	c) $\frac{1}{16}$	d) $\frac{1}{8}$ G	
12.	If $\cos A = \frac{\sqrt{3}}{2}$, $0^{\circ} < A < 90^{\circ}$, then A is equal to	b) 1	[1]
	a) 30°	b) 1	
	c) $\frac{\sqrt{3}}{2}$	d) 60°	
13.	At some time of the day, the height and length of the s	hadow of a man are equal. The sun's altitude is:	[1]
	a) 45°	b) 30°	
	c) 900	d) 60°	
14.	A horse is grazing in a field. It is tied to a pole with a B making an arch with an angle of 70°. Find the area o	rope of length 6 m. The horse moves from point A to point of the sector grazed by the horse.	[1]
	a) 22.99 m	b) 20.99 m	
	c) 21.99 m	d) 21 m	
15.		er has a blade of length 42 cm sweeping through an angle	[1]
	of 120 ⁰ . Find the total area cleaned at each sweep of t		
	a) 5544 cm ²	b) 3696 cm ²	
	c) ₄₂₂₄ cm ²	d) 1848 cm ²	
16.	An event is unlikely to happen. Its probability is close	st to	[1]
	a) 0.00001	b) 0.0001	
15	c) 0.1		641
17.	One card is drawn at random from a well-shuffled dec		[1]
	a) $\frac{1}{13}$	b) $\frac{3}{26}$	
	c) $\frac{1}{52}$	d) $\frac{4}{52}$	
		of 19	
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18.	If every term of the statistical data consisting of n ter	rms is decreased by 2, then the mean of the data:	[1]
	a) decreases by 1	b) remains unchanged	
	c) decreases by 2	d) decreases by 2n	
19.	Assertion (A): Two identical solid cubes of side 5 c	m are joined end to end. The total surface area of the	[1]
	resulting cuboid is 350 cm ² .		
	Reason (R): Total surface area of a cuboid is 2(lb +	bh + hl)	
	a) Both A and R are true and R is the correct explanation of A.	b) Both A and R are true but R is not the correct explanation of A.	
	c) A is true but R is false.	d) A is false but R is true.	
20.	Assertion (A): Common difference of the AP -5, -1,	3, 7, is 4.	[1]
	Reason (R): Common difference of the AP a, a + d,	a + 2d, is given by $d = 2nd$ term - 1st term.	
	a) Both A and R are true and R is the correct explanation of A.	b) Both A and R are true but R is not the correct explanation of A.	
	c) A is true but R is false.	d) A is false but R is true.	
	Se	ection B	
21.	Prove that 5 + 2 $\sqrt{3}$ is an irrational number, given the		[2]
22.		ely of a $\triangle ABC$ such that $DE BC$ and BD = CE. Prove that	[2]
23.	Δ ABC is isosceles.	a circle with centre O and OP cuts the circle at T and QOR	[2]
	is a diameter. If $\angle POR = 130^{\circ}$ and S is a point on the second seco	e circle, find $\angle 1 + \angle 2$.	
24.	Prove that: $\sqrt{rac{1+\sin A}{1-\sin A}}= \sec A + an A$		[2]
		OR	
	If $m \sin A + n \cos A = p$ and $m \cos A - n \sin A = q$, pro-	by that $m^2 + n^2 = p^2 + q^2$.	
25.	In a circle of radius 21 cm, an arc subtends an angle	of 60° at the centre. Find the area of the sector formed by	[2]
	the arc. Also, find the length of the arc.		
		OR	
	If a chord of a circle of radius 10 cm subtends an ang corresponding minor segment of the circle. (Use π =	gle of 60° at the centre of the circle, find the area of the	
		ection C $(3.14 \text{ and } \sqrt{3} - 1.73)$	
26.	If two positive integers p and q are written as $p = a^2 l$		[3]
20.	Verify.LCM \times (p.q.) \times HCF (p.q.) = pq		
27.	If α , β are the zeroes of the x ² + 7x + 7, find the value	we of $rac{1}{lpha}+rac{1}{eta}-2lphaeta.$	[3]
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28. Find the sum of all the natural numbers less than 100 which are divisible by 6.

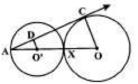
OR

The ratio of the sums of first m and first n terms of an A.P. is $m^2 : n^2$. Show that the ratio of its m^{th} and n^{th} terms is (2m - 1):(2n - 1).

29. In two concentric circles, a chord of length 8 cm of the larger circle touches the smaller circle. If the radius of the larger circle is 5 cm then find the radius of the smaller circle.

OR

Equal circles with centres O and O' touch each other at X. OO' produced to meet a circle with centre O', at A. AC is a tangent to the circle whose centre is O. O' D is perpendicular to AC. Find the value of $\frac{DO'}{CO}$.



average speed?

- 30. If $\tan \theta + \frac{1}{\tan \theta} = 2$, find the value of $\tan^2 \theta + \frac{1}{\tan^2 \theta}$
- 31. The weights (in kg) of 50 wild animals of a National Park were recorded and the following data was obtained: [3]

Weight (in kg)	Number of animals	
100 - 110	4	
110 - 120	12	
120 - 130	23	
130 - 140	8	
140 - 150	3	

Find the mean weight (in kg) of animals, using assumed mean method.

Section D

OR

32. The difference of two numbers is 5 and the difference of their reciprocals is $\frac{1}{10}$. Find the numbers.

A train travels at a certain average speed for a distance 63 km and then travels a distance of 72 km at an average speed of 6 km/hr more than the original speed. If it takes 3 hours to complete total journey, what is its original

- A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. [5]
 The angle of elevation of the balloon from the eyes of the girl at any instant is 60°. After some time, the angle of elevation reduces to 30°. Find the distance travelled by the balloon during the interval.
- 34. A spherical glass vessel has a cylindrical neck 8 cm long and 1 cm in radius. The radius of the spherical part is 9 **[5]** cm. Find the amount of water (in litres) it can hold, when filled completely.

OR

The boilers are used in thermal power plants to store water and then used to produce steam. One such boiler consists of a cylindrical part in middle and two hemispherical parts at its both ends. Length of the cylindrical part is 7m and radius of cylindrical part is $\frac{7}{2}$ m.

Find the total surface area and the volume of the boiler. Also, find the ratio of the volume of cylindrical part to the

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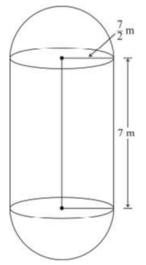


[3]

[3]

[5]

volume of one hemispherical part.



35. Find the mode, median and mean for the following data:

Marks Obtained	25 - 35	35 - 45	45 - 55	55 - 65	65 - 75	75 - 85
Number of students	7	31	33	17	11	1

Section E

36. Read the following text carefully and answer the questions that follow:

A coaching institute of Mathematics conducts classes in two batches I and II and fees for rich and poor children are different. In batch I, there are 20 poor and 5 rich children, whereas in batch II, there are 5 poor and 25 rich children. The total monthly collection of fees from batch I is ₹ 9000 and from batch II is ₹ 26,000. Assume that each poor child pays ₹ x per month and each rich child pays ₹ y per month.



- i. Represent the information given above in terms x and y. (1)
- ii. Find the monthly fee paid by a poor child. (1)
- iii. Find the difference in the monthly fee paid by a poor child and a rich child. (2)

OR

If there are 10 poor and 20 rich children in batch II, what is the total monthly collection of fees from batch II? (2)

37. Read the following text carefully and answer the questions that follow:

[4]

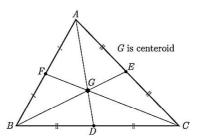
The centroid is the centre point of the object. It is also defined as the point of intersection of all the three medians. The median is a line that joins the midpoint of a side and the opposite vertex of the triangle. The centroid of the triangle separates the median in the ratio of 2 : 1. It can be found by taking the average of x-coordinate points and y-coordinate points of all the vertices of the triangle. See the figure given below

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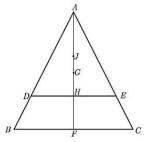


[5]

[4]



Here D, E and F are mid points of sides BC, AC and AB in same order. G is centroid, the centroid divides the median in the ratio 2 : 1 with the larger part towards the vertex. Thus AG : GD = 2 : 1 On the basis of above information read the question below. If G is Centroid of \triangle ABC with height h and J is Centroid of \triangle ADE. Line DE parallel to BC, cuts the \triangle ABC at a height $\frac{h}{4}$ from BC. HF = $\frac{h}{4}$



i. What is the length of AH? (1)

- ii. What is the distance of point A from point G? (1)
- iii. What is the distance of point A from point J? (2)

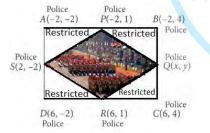
OR

What is the distance GJ? (2)

38. Read the following text carefully and answer the questions that follow:

In order to facilitate smooth passage of the parade, movement of traffic on certain roads leading to the route of the Parade and Tableaux ah rays restricted. To avoid traffic on the road Delhi Police decided to construct a rectangular route plan, as shown in the figure.

[4]



- i. If Q is the mid point of BC, then what are the coordinates of Q? (1)
- ii. What is the length of the sides of quadrilateral PQRS? (2)
- iii. What is the length of route PQRS? (2)

OR

What is the length of route ABCD? (2)

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XI AMU ENTRANCE RESULTS 2023-24

Abhishek Gaur

Aaliya Singh

Mugdha Singh

Tanmay Mudgal Aastha Sharma











Riddhima Tomar

Shaurya Gangal

Ayushi Gautam

Anubhav Gupta Akash Basu





Rashi Singh





Saloni Chaudhary Ayushi Dhanger



Sanchi Popli



Yashi Vashishtha



Harshit Raghav



Divya Singh



Srishty











Vanshika Garg







Sanyogita



Vivek Gautam















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Khanak









Prachi Singh









Pakhi Garg

Prabhat Singh



Manav Kushwaha









Rudraksh Chaudhary

Ayush Senger

Aryan Tiwari

Afifa Malik







Solution

```
Section A
```

1.

(d) 120 **Explanation:** Least positive integer divisible by 20 and 24 is LCM of (20, 24).

 $20 = 2^2 \times 5$

 $24 = 2^3 \times 3$

: LCM (20, 24) = $2^3 \times 3 \times 5 = 120$ Thus 120 is divisible by 20 and 24.

2.

(c) a < 0, b < 0 and c > 0

Explanation: Clearly, $f(x) = ax^2 + bx + c$ represent a parabola opening downwards. Clearly a < 0

Let, $y = ax^2 + bx + c$ cuts y-axis at P which lies on OY.

Putting x = 0 in $y = ax^2 + bx + c$, we get y = c. So the coordinates of P are (0, c).

Clearly, P lies on OY. Therefore c > 0The vertex $\left(\frac{-b}{2a}, \frac{-D}{4a}\right)$ of the parabola is in the second quadrant.

Therefore, $\frac{-b}{2a} < 0$, b < 0

Therefore a < 0, b < 0 and c > 0.

3.

(d) 0

Explanation: The number of solutions of two linear equations representing parallel lines is 0 because two linear equations representing parallel lines has no solution and they are inconsistent.

4.

5.

(c) pq

Explanation: Let the roots of given quadratic equation be α and β .

```
On comparing equation x^2 - (p - q)x + k = 0
with ax^2 + bx + c = 0, we have
a = 1, b = -(p + q), c = k
We know that
\Rightarrow \alpha + \beta = \frac{-b}{a}
Put the value a and b
\Rightarrow \alpha + \beta = \frac{p+q}{1}
\Rightarrow \alpha + \beta = p + q \dots (i)
Given \alpha = p
Put the value of \alpha in equation (i),
\Rightarrow p + \beta = p + q
\Rightarrow \beta = q
But we know that
\alpha \cdot \beta = \frac{c}{a}
Put the values
p.q. =\frac{k}{1}
Then, k = pq.
(d) 28
```

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```
Explanation: Given: d = -4, n = 7 and a_n = 4
               a_n = a + (n - 1)d
                \Rightarrow 4 = a + (7 - 1) \times (-4)
                \Rightarrow 4 = a + 6 \times -4
                \Rightarrow 4 = a - 24
                \Rightarrow a = 28
               (a) 12 units
        6.
               Explanation: 12 units
        7.
                (b) (-1, -8)
                Explanation: (-1, -8)
               (a) 4.5
        8.
               Explanation: \angle ADE = \angle ABC and \angle DAE = \angle BAC. Hence \triangle ADE \sim \triangle ABC (AA similarity)
                hence the corresponding sides are in proportion
               \frac{AD}{AB} = \frac{AE}{Ac}\Rightarrow \frac{2}{5} = \frac{3}{CE+3}
                \Rightarrow CE = 4.5
        9.
               (a) 30°
               Explanation: \angle OAB = 60^{\circ} (given)
                \angle OAB = \angle OBA (:: OA = OB = r)
               ∴∠OBA = 60°
                Now, in \triangle OAB
                \angle AOB = 180^{\circ} - 60^{\circ} - 60^{\circ}
                \angle AOB = 60^{\circ}
                Now, In \triangle AOP
                \angle OPA + \angle OAP + \angle AOP = 180^{\circ} (angle sum property of \triangle)
                \angle OPA + 90^{\circ} + 60^{\circ} = 180^{\circ}
                \angle OPA = 180^{\circ} - 150^{\circ}
                \angle OPA = 30^{\circ}
      10.
                (b) one point only
                Explanation: one point only
               (a) \frac{1}{2}
       11.
               Explanation: We know that \sec^2 A - \tan^2 A = 1.

\therefore (2x)^2 - \left(\frac{2}{x}\right)^2 = 1 \Rightarrow 4x^2 - \frac{4}{x^2} = 1 \Rightarrow 4\left(x^2 - \frac{1}{x^2}\right) = 1
               \Rightarrow \left(x^2 - \frac{1}{x^2}\right) = \frac{1}{4} \Rightarrow 2\left(x^2 - \frac{1}{x^2}\right) = 2 \times \frac{1}{4} = \frac{1}{2}
               (a) 30°
       12.
               Explanation: Cos A = \frac{\sqrt{3}}{2}
                \cos A = \cos 30^{\circ}
               A = 30^{\circ}
               (a) 45<sup>0</sup>
       13.
                Explanation: 45°
       14.
                (c) 21.99 m
               Explanation: The area of the sector =rac{x^\circ}{360^\circ}	imes\pi r^2
                                                                                      Page 9 of 18
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$$=rac{70^{\circ}}{360^{\circ}} imesrac{22}{7} imes 6^{2}$$

21.99 m

15.

(b) 3696 cm²

Explanation: Clearly, each wiper sweeps a sector of a circle of radius 42 cm and sector angle 120°.

 \therefore Total area cleaned at each sweep = $2 \times \frac{\theta}{360^\circ} \times \pi r^2$

= $2 \times \frac{120^{\circ}}{360^{\circ}} \times \frac{22}{7} \times 42 \times 42 \text{ cm}^2$ = 3696 cm²

(a) 0.00001 16.

Explanation: An event is unlikely to happen. Its probability is very very close to zero but not zero, So it is equal to 0.00001

17. (a) $\frac{1}{13}$

> **Explanation:** Total number of cards = 52. Number of 6 s = 4. : P (getting a 6) = $\frac{4}{52} = \frac{1}{13}$

18.

(c) decreases by 2

Explanation: decreased by 2.

19.

(d) A is false but R is true. **Explanation:** A is false but R is true.

of A. 20. (a) Both A and R are true and R is the correct explanation of A. **Explanation:** Common difference, d = -1 - 1(-5) = 4So, both A and R are true and R is the correct explanation of A.

Section B

21. Given

 $\sqrt{3}$ is an irrational number Let 5 + $2\sqrt{3}$ is a rational number : we can write $5 + 2\sqrt{3} = \frac{p}{q}$, where p and q are integers

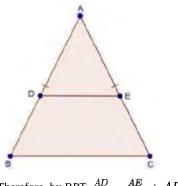
$$\Rightarrow 2\sqrt{3} = \frac{p}{q} - 5 = \frac{p}{q}$$

Here, $\frac{p-5q}{2q}$ is a rational number So, $\sqrt{3}$ is also a rational number. But it is given that $\sqrt{3}$ is irrational number.

 \Rightarrow our assumption was wrong

 \Rightarrow 5 + 2 $\sqrt{3}$ is an irrational number.

22. We have, DE || BC



Therefore, by BPT, $\frac{AD}{BD}=\frac{AE}{EC}$ \Rightarrow AD=AEAdding DB on both sides \Rightarrow AD + DB = AE + DB \Rightarrow AD + DB = AE + EC [\therefore BD = CE]

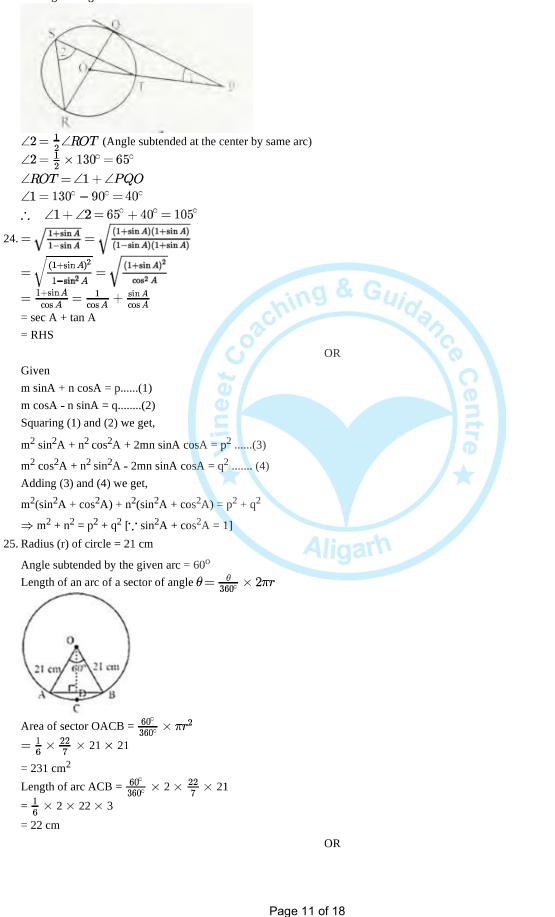
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 $\Rightarrow AB = AC$

 $\therefore \Delta$ ABC is isosceles triangle.

```
23. In the given figure
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Area of minor segment = $\frac{3.14 \times (10)^2 \times 60^\circ}{360^\circ} - \frac{1}{2} \times (10)^2 \times \frac{\sqrt{3}}{2}$ = $\frac{314}{6} - \frac{173}{4}$ = $9\frac{1}{12}$ or 9.08

Hence, area of minor segment is 9.08 cm^2 .

Section C

26. Given, $p = a^2 b^3$ and $q = a^3 b$ $HCF(p,q) = a^2b$ $LCM(p, q) = a^3b^3$ $pq = a^2b^3 \times a^3b = a^5b^4$ ----(1) $LCM(p,q) \times HCF(p,q) = a^{3}b^{3} \times a^{2}b = a^{5}b^{4} - - - - (2)$ From equation (1) and (2) We get $LCM(p,q) \times HCF(p,q) = pq$ 27. Let the given polynomial is $p(x) = x^2 + 7x + 7$ Here,a = 1, b = 7, c = 7 $\therefore \alpha, \beta$ are both zeroes of p(x) $\therefore \quad \alpha + \beta = \frac{-b}{a} = -7$(i) $\alpha\beta = \frac{c}{a} = 7$ (ii) Now, $\frac{\frac{1}{\alpha} + \frac{1}{\beta} - 2\alpha\beta = \frac{\beta + \alpha}{\alpha\beta} - 2\alpha\beta }{= \frac{-7}{7} - 2 \times 7 }$ = -1 - 14 = -15 Hence the value of $\frac{1}{\alpha} + \frac{1}{\beta} - 2\alpha\beta$ is - 15. 28. All the natural numbers less than 100 which are divisible by 6 are 6, 12, 18, 24,...., 96 Here, $a_1 = 6$ $a_2 = 12$ $a_3 = 18$ $a_4 = 24$:: $\therefore a_2 - a_1 = 12 - 6 = 6$ $a_3 - a_2 = 18 - 12 = 6$ $a_4 - a_3 = 24 - 18 = 6$ $a_2 - a_1 = a_3 - a_2 = a_4 - a_3 = 6$ (=6 in each case) : This sequence is an arithmetic progression whose difference is 6. Here, a = 6d = 6 1 = 96Let the number of terms be n. Then, l = a + (n - 1)d \Rightarrow 96 = 6 + (n - 1)6 \Rightarrow 96 - 6 = (n - 1)6 \Rightarrow 90 = (n - 1)6 \Rightarrow (n - 1)6 = 90 $\Rightarrow n-1=\frac{90}{6}$ \Rightarrow n - 1 = 15 \Rightarrow n = 15 + 1 \Rightarrow n = 16 Page 12 of 18

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$$\therefore S_n = \frac{n}{2}(a+l)$$
$$= \left(\frac{16}{2}\right)(6+96)$$
$$= (8) (102)$$
$$= 816$$

OR

Let first term of given A.P. be a and common difference be d also sum of first m and first n terms be S_m and S_n respectively

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Let the radius of both the circles is r.
In the fig. OD_LAC and AC is tangent of circle (O,r)
So, OC
$$\perp$$
 AC (as line joining center to tangent is \perp to the tangent)
Now in ΔAOD and ΔAOC ,
 $\angle ODA = \angle OCA = 90^{\circ}$
 $\angle A = \angle A$ (common)
Therefore, $\Delta AOD \sim \Delta AOC$ (by AA rule]
So, $\frac{DO}{CO} = \frac{AO}{AO}$(1)
Now, AO = r + r + r = 3r
and O'A = r
Putting the value of AO and AO' in equation (1), we get
 $\frac{DO}{CO} = \frac{r}{s} = \frac{1}{3}$
Therefore, DO':CO = 1:3
30. We have,
 $\tan \theta + \frac{1}{\tan^2}\theta = 2$
Squaring both sides, we get
 $\Rightarrow (\tan \theta + \frac{1}{\tan^2}\theta + 2 \approx \tan \theta \times \frac{1}{\tan \theta} = 4$
 $\Rightarrow \tan^2 \theta + \frac{1}{\tan^2}\theta + 2 \approx 4$
 $\Rightarrow \tan^2 \theta + \frac{1}{\tan^2}\theta = 2$
Alternate method, We have
 $\tan \theta + \frac{1}{\tan^2}\theta = 2$
 $\Rightarrow \tan^2 \theta - 2\tan \theta + 1 = 0$
 $\Rightarrow \tan^2 \theta - 2\tan \theta + 1 = 0$
 $\Rightarrow \tan^2 \theta - 1 = 2 \tan \theta$
 $\Rightarrow \tan^2 \theta - 1 = 2 \tan \theta$
 $\Rightarrow \tan^2 \theta - 1 = 1 + 1 = 2$
31. Weight (in kg) (Class Interval) Number of animals (f₁) Mid point (x₁)
100-110 4 105

1.	Weight (in kg) (Class Interval)	Number of animals (f _i)	Mid point (x _i)	d _i = x _i - a	$f_i d_i$
	100-110	4 Aligan	105	-20	-80
	110-120	12	115	-10	-120
	120-130	23	125	0	0
	130-140	8	135	10	80
	140-150	3	145	20	60
	Total	50			-60

let a= 125,
$$\sum f_i$$
 = 50, $\sum f_i d_i$ = 60

Now, Mean = a $f_i d_i$ (-60)Mean = 125 + -50Mean = 125 - 1.2 Mean = 123.8

Section D

32. Let the first number be x

 \therefore Second number = x + 5

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Now according to the question

 $\frac{1}{x} - \frac{1}{x+5} = \frac{1}{10}$ $\Rightarrow \frac{x+5-x}{x(x+5)} = \frac{1}{10}$ $\Rightarrow 50 = x^2 + 5x$ $\Rightarrow x^2 + 5x - 50 = 0$ $\Rightarrow x^2 + 10x - 5x - 50 = 0$ $\Rightarrow x(x+10) - 5(x+10) = 0$ $\Rightarrow (x+10)(x-5) = 0$ x = 5, -10 rejectedThe numbers = 5 and 10.

OR

Let the original average speed of the train be x km/hr. Time taken to cover 63 km = $\frac{63}{x}$ hours

Time taken to cover 72 km when the speed is increased by 6 km/hr = $\frac{72}{x+6}$ hours By the question, we have,

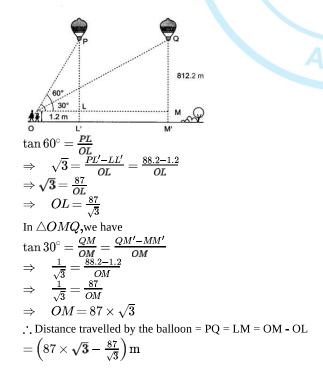
 $\frac{63}{x} + \frac{72}{x+6} = 3$ $\Rightarrow \frac{21}{x} + \frac{24}{x+6} = 1$ $\Rightarrow \frac{21x+126+24x}{x^2+6x} = 1$ $\Rightarrow 45x + 126 = x^2 + 6x$ $\Rightarrow x^2 - 39x - 126 = 0$ $\Rightarrow x^2 - 42x + 3x - 126 = 0$ $\Rightarrow x(x - 42) + 3(x - 42) = 0$ $\Rightarrow (x - 42)(x + 3) = 0$ $\Rightarrow x - 42 = 0 \text{ or } x + 3 = 0$ $\Rightarrow x = 42 \text{ or } x = -3$

Since the speed cannot be negative, $x \neq -3$.

Thus, the original average speed of the train is 42 km/hr.

33. Let P be the position of the balloon when its angle of elevation from the eyes of the girl is 60° and Q be the position when angle of elevation is 30°.

In $\triangle OLP$, we have



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$$= 87 \times \left(\sqrt{3} - \frac{1}{\sqrt{3}}\right) \mathbf{m} = \frac{87 \times 2}{\sqrt{3}} \mathbf{m} = \frac{174}{\sqrt{3}} \mathbf{m}$$
$$= \frac{174}{3} \sqrt{3} \mathbf{m} = 58 \sqrt{3} \mathbf{m}.$$

34. The volume of the spherical vessel is

calculated by the given formula

V = $\frac{4}{3}\pi \times r^3$ Now, $V = \frac{4}{3} \times \frac{22}{7} \times 9 \times 9 \times 9$

 $V = 3,054.85 \text{ cm}^3$

The volume of the cylinder neck is calculated by the given formula.

V = $\pi imes R^2 imes h$ Now, $V = \frac{22}{7} \times 1 \times 1 \times 8$

 $V = 25.14 \text{ cm}^3$

The total volume of the vessel is equal to the volume of the spherical shell and the volume of its cylindrical neck.

OR

& Guidance

 $3054.85 + 25.14 = 3,080 \text{ cm}^3$

The total volume of the vessel is $3,080 \text{ cm}^3$.

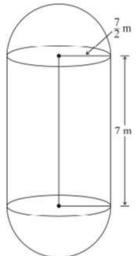
As we know,

 $1 L = 1000 cm^3$

 $\frac{3080}{1000} = 3.080 \text{ L}$

Thus, the amount of water (in litres) it can hold is 3.080 L.

Given that,



Length of cylindrical part = 7 m Radius of cylindrical part = $\frac{7}{2}$ m

Total surface area of figure = $2\pi rh + 2(2\pi r^2)$

$$=2\pi\left[rac{7}{2} imes 7+2 imes\left(rac{7}{2}
ight)^2
ight]$$

 $= 308 \text{ m}^2$

Volume of boiler = Volume of cylindrical part + Volume of two hemispherical parts

$$= \pi r^{2}h + \left(\frac{4}{3}\right)\pi r^{3}$$

$$= \pi \left(\frac{7}{2}\right)^{2} \times (7) + \left(\frac{4}{3}\right)\pi \left(\frac{7}{2}\right)^{3}$$

$$= 269.5 + 179.66$$

$$= 449.167 m^{3}$$
Required ratio =
$$\frac{\text{Volume of cylindrical part}}{\text{Volume of one hemispherical part}}$$

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$$=\frac{269.5}{89.83}$$

= 3

35. Table:

· .	. 101.						
	Class	Frequency	Mid value x _i	f _i x _i	Cumulative frequency		
	25 - 35	7	30	210	7		
	35 - 45	31	40	1240	38		
	45 - 55	33	50	1650	71		
	55 - 65	17	60	1020	88		
	65 - 75	11	70	770	99		
	75 - 85	1	80	80	100		
		N = 100		$\sum f_i x_i = 4970$			

i. Mean

 $\frac{\sum f_i x_i}{\sum f_i} = \frac{4970}{100} = 49.70$ ii. N = 100, $\frac{N}{2} = 50$

Median Class is 45 - 55

l = 45, h = 10, N = 100, c = 38, f = 33

$$\therefore$$
 Median = $l + h \left(\frac{N}{2} \right)$

$$=45+\left\{10\times\frac{50-38}{22}\right\}$$

$$=45+3.64=48.64$$

ching & Guidance iii. we know that, Mode = $3 \times \text{median} = 2 \times \text{mean}$

```
= 3 \times 48.64 - 2 \times 49.70
```

= 145.92 - 99.4 = 46.52

```
36. i. Since, each poor child pays ₹ x
       and each rich child pays ₹ y
```

Section E

∴ In batch I, 20 poor and 5 rich children pays ₹ 9000 can be represented as 20x + 5y = 9000and in batch II, 5 poor and 25 rich children pays ₹ 26,000 can be represented as 5x + 25y = 26,000 ii. As we have 20x + 5y = 9,000 ...(i)

and 5x + 25y = 26,000

or x + 5y = 5,200 ...(ii)

On subtracting (ii) from (i), we get 19x = 3,800

```
\Rightarrow x = 200
```

∴ Monthly fee paid by a poor child = ₹ 200

```
iii. As we have,
```

```
20x + 5y = 9000 \dots (i)
and 5x + 25y = 26000
```

```
x + 5y = 5200 \dots (ii)
```

On subtracting equation (ii) from (i), we have

$$19x = 3800$$

 $x = \frac{3800}{19}$

= 200

```
Put the value of x in equation (ii), we get
```

```
200 + 5y = 5200
```

5y = 5200 - 200

y = 1000

```
∴ y - x = 1000 - 200
```

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= 800 Hence, difference in the monthly fee paid by a poor child and a rich child is ₹ 800. OR Total monthly fee = 10x + 20y= 10(200) + 20(1,000)= 2,000 + 20,000 =₹22,000 37. i. ∴ AF = h (Given) $\therefore AF = AH + HF$ $h = AH + \frac{h}{4}$ $AH = h - \frac{h}{4}$ $AH = \frac{3h}{4}$ ii. : AF = h (Given) $\therefore AG = \frac{2}{3} AF$: centroid divide the median in 2 : 1 iii. AH = $\frac{3h}{4}$ J is centroid of $\triangle ADE$ AJ : JH = 2 : 1let AJ = 2x and JH = x $2\mathbf{x} + \mathbf{x} = \frac{3h}{4}$ $x = \frac{h}{4}$ $AJ = 2 \times \frac{h}{4} = \frac{h}{2}$ AG = AJ + GJ $= \frac{h}{2} + \frac{h}{6}$ $= \frac{2h}{3}$ But AJ = $\frac{h}{2} \times \frac{2}{3}$ $AJ = \frac{3}{4}AG$ OR GJ = AG - AJ= AG - $\frac{3}{4}$ AG $GJ = \frac{1}{4} \overline{AG}$ 38. i. Q(x, y) is mid-point of B(-2, 4) and C(6, 4) \therefore (x, y) = $\left(\frac{-2+6}{2}, \frac{4+4}{2}\right) = \left(\frac{4}{2}, \frac{8}{2}\right) = (2, 4)$ ii. Since PQRS is a rhombus, therefore, PQ = QR = RS = PS. : PQ = $\sqrt{(-2-2)^2 + (1-4)^2} = \sqrt{16+9} = \sqrt{25} = 5$ units Thus, length of each side of PQRS is 5 units. iii. Length of route PQRS = 4 PQ $= 4 \times 5 = 20$ units OR Length of CD = 4 + 2 = 6 units and length of AD = 6 + 2 = 8 units : Length of route ABCD - 2(6 + 8) = 28 units