

**Class X Session 2024-25**  
**Subject - Mathematics (Basic)**  
**Sample Question Paper - 1**

**Time Allowed: 3 hours**

**Maximum Marks: 80**

**General Instructions:**

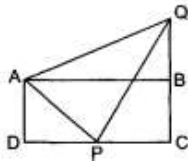
1. This Question Paper has 5 Sections A, B, C, D and E.
2. Section A has 20 MCQs carrying 1 mark each
3. Section B has 5 questions carrying 02 marks each.
4. Section C has 6 questions carrying 03 marks each.
5. Section D has 4 questions carrying 05 marks each.
6. Section E has 3 case-based integrated units of assessment carrying 04 marks each.
7. All Questions are compulsory. However, an internal choice in 2 Qs of 5 marks, 2 Qs of 3 marks and 2 Questions of 2 marks has been provided. An internal choice has been provided in the 2 marks questions of Section E
8. Draw neat figures wherever required. Take  $\pi = \frac{22}{7}$  wherever required if not stated.

**Section A**

1. The HCF of 95 and 152, is [1]
  - a) 57
  - b) 19
  - c) 38
  - d) 1
2. Given that H.C.F. (306, 954, 1314) = 18, find L.C.M. (306, 954, 1314). [1]
  - a) 1183234
  - b) 1123328
  - c) 1183914
  - d) 1123238
3. If  $x = 3$  is a solution of the equation  $3x^2 + (k - 1)x + 9 = 0$  then  $k = ?$  [1]
  - a) 13
  - b) -11
  - c) 11
  - d) -13
4. The angles of a triangle are  $x^\circ$ ,  $y^\circ$  and  $40^\circ$ . The difference between the two angles  $x$  and  $y$  is  $30^\circ$ , then [1]
  - a)  $x^\circ = 75^\circ$  and  $y^\circ = 45^\circ$
  - b)  $x^\circ = 85^\circ$  and  $y^\circ = 55^\circ$
  - c)  $x^\circ = 95^\circ$  and  $y^\circ = 35^\circ$
  - d)  $x^\circ = 65^\circ$  and  $y^\circ = 95^\circ$
5.  $x^2 - 6x + 6 = 0$  have [1]
  - a) Real and Equal roots
  - b) Real roots
  - c) No Real roots
  - d) Real and Distinct roots
6. Two vertices of  $\triangle ABC$  are A (-1, 4) and B(5, 2) and its centroid is G(0, -3). Then, the coordinates of C are [1]







23. Prove that the tangents drawn at the ends of a diameter of a circle are parallel. [2]
24. If  $\operatorname{cosec}^2\theta(1 + \cos\theta)(1 - \cos\theta) = \lambda$ , then find the value of  $\lambda$ . [2]
25. To warn ships for underwater rocks, a lighthouse spreads a red coloured light over a sector of angle  $80^\circ$  to a distance of 16.5 km. Find the area of the sea over which the ships are warned. (use  $\pi = 3.14$ ) [2]

OR

What is the angle subtended at the centre of a circle of radius 6 cm by an arc of length  $3\pi$  cm?

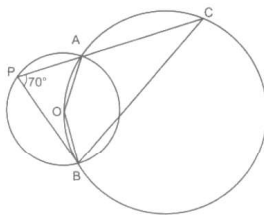
### Section C

26. Prove that  $\sqrt{5}$  is irrational. [3]
27. If  $\alpha, \beta$  are zeroes of the quadratic polynomial  $x^2 + 9x + 20$ , form a quadratic polynomial whose zeroes are  $(\alpha + 1)$  and  $(\beta + 1)$ . [3]
28. Solve the pair of linear equations  $\sqrt{2}x - \sqrt{3}y = 0$  and  $\sqrt{3}x - \sqrt{8}y = 0$  by substitution method. [3]

OR

Aditya is walking along the line joining points (1,4) and (0,6). Aditi is walking along the line joining points (3,4) and (1,0). Represent the graph and find the point where both cross each other.

29. In a given figure, two circles intersect at A and B. The centre of the smaller circle is O and it lies on the circumference of the larger circle. If  $\angle APB = 70^\circ$ , find  $\angle ACB$ . [3]



30. In  $\triangle PQR$ , right angled at Q,  $PR + QR = 25$  cm and  $PQ = 5$  cm. Determine the values of  $\sin P$ ,  $\cos P$  and  $\tan P$ . [3]

OR

Prove that:  $\frac{\cos^3\theta + \sin^3\theta}{\cos\theta + \sin\theta} + \frac{\cos^3\theta - \sin^3\theta}{\cos\theta - \sin\theta} = 2$ .

31. One card is drawn from a well-shuffled deck of 52 cards. Find the probability of getting [3]
- a king of red colour
  - a face card
  - a red face card
  - the jack of hearts
  - a spade
  - the queen of diamonds

### Section D

32. Solve for x:  $\left(\frac{2x}{x-5}\right)^2 + 5\left(\frac{2x}{x-5}\right) - 24 = 0, x \neq 5$  [5]

OR

The sum of squares of two consecutive multiples of 7 is 637. Find the multiples.

33. Sides AB and AC and median AD of a triangle ABC are respectively proportional to sides PQ and PR and median PM of another triangle PQR. Show that  $\triangle ABC \sim \triangle PQR$ . [5]
34. A solid is in the shape of a hemisphere surmounted by a cone. If the radius of hemisphere and base radius of [5]

cone is 7 cm and height of cone is 3.5 cm, find the volume of the solid. (Take  $\pi = \frac{22}{7}$ )

OR

A solid toy is in the form of a hemisphere surmounted by a right circular cone. Height of the cone is 2 cm and the diameter of the base is 4 cm. If a right circular cylinder circumscribes the solid. Find how much more space it will cover.

35. The following data gives the distribution of total monthly household expenditure of 200 families of a village. [5]

Find the modal monthly expenditure of the families. Also, find the mean monthly expenditure:

Expenditure (in ₹)	Frequency
1000-1500	24
1500-2000	40
2000-2500	33
2500-3000	28
3000-3500	30
3500-4000	22
4000-4500	16
4500-5000	7

Section E

36. Read the following text carefully and answer the questions that follow: [4]

Kamla and her husband were working in a factory in Seelampur, New Delhi. During the pandemic, they were asked to leave the job. As they have very limited resources to survive in a metro city, they decided to go back to their hometown in Himachal Pradesh. After a few months of struggle, they thought to grow roses in their fields and sell them to local vendors as roses have been always in demand. Their business started growing up and they hired many workers to manage their garden and do packaging of the flowers.



In their garden bed, there are 23 rose plants in the first row, 21 are in the 2<sup>nd</sup>, 19 in 3<sup>rd</sup> row and so on. There are 5 plants in the last row.

- How many rows are there of rose plants? (1)
- Also, find the total number of rose plants in the garden. (1)
- How many plants are there in 6th row. (2)

OR

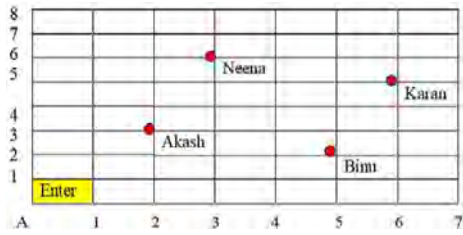
If total number of plants are 80 in the garden, then find number of rows? (2)

37. Read the following text carefully and answer the questions that follow: [4]

Karan went to the Lab near to his home for COVID 19 test along with his family members.

The seats in the waiting area were as per the norms of distancing during this pandemic (as shown in the figure).

His family member took their seats surrounded by red circular area.

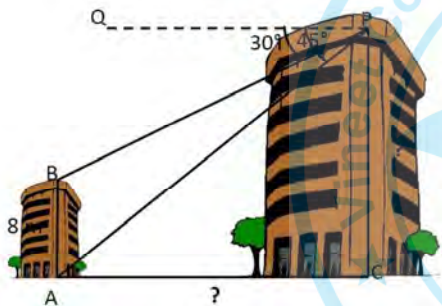


- i. What is the distance between Neena and Karan? (1)
- ii. What are the coordinates of seat of Akash? (1)
- iii. What will be the coordinates of a point exactly between Akash and Binu where a person can be? (2)

**OR**

Find distance between Binu and Karan. (2)

38. Basant and Vinod lives in a housing society in Dwarka, New Delhi. There are two building in their housing society. The first building is 8 meter tall. One day, both of them were just trying to guess the height of the other multi-storeyed building. Vinod said that it might be a 45 degree angle from the bottom of our building to the top of multi-storeyed building so the height of the building and distance from our building to this multi-storeyed building will be same. Then, both of them decided to estimate it using some trigonometric tools. Let's assume that the first angles of depression of the top and bottom of an 8 m tall building from top of a multi-storeyed building are  $30^\circ$  and  $45^\circ$ , respectively. [4]



- i. Now help Vinod and Basant to find the height of the multi-storeyed building.
- ii. Also, find he distance between two buildings.





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**Kanika Garg**



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**Prabhat Singh**



**Anubhav Gupta**



**Akash Basu**



**Shaurya Gangal**



**Abhishek Gaur**



**Rudraksh Chaudhary**



**Aryan Tiwari**



**Pakhi Garg**



**Rashi Singh**



**Ragini Singh**



**Pratishtha Sharma**



**Aaliya Singh**



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**Yashika**



**Manav Kushwaha**



**Saloni Chaudhary**



**Ayushi Dhanger**



**Ayushi Gautam**



**Mugdha Singh**



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**Sanchi Popli**



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**Prisha Tanwar**



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**Sanyogita**



**Aakash Sharma**



**Ipshita Upadhyay**



**Yashi Vashishtha**



**Divya Singh**



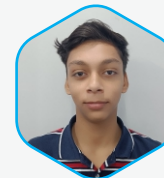
**Karnika Singh**



**Harshit Chaudhary**



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**Lalit Dhargar**



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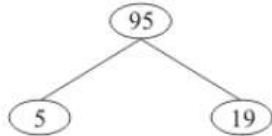
# Solution

## Section A

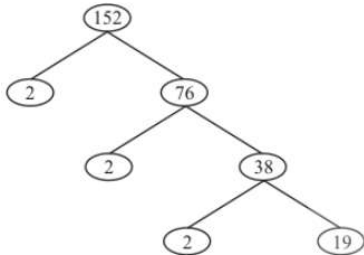
1.

(b) 19

**Explanation:** Using the factor tree for 95, we have:



Using the factor tree for 152, we have:



Therefore,

$$95 = 5 \times 19$$

$$152 = 2^3 \times 19$$

$$\text{HCF}(95, 152) = 19$$

2.

(c) 1183914

**Explanation:** L.C.M. (306, 954, 1314)

$$= \frac{306 \times 954 \times 1314 \times \text{H.C.F.}(306, 954, 1314)}{\text{H.C.F.}(306, 954) \times \text{H.C.F.}(954, 1314) \times \text{H.C.F.}(306, 1314)}$$
$$= \frac{306 \times 954 \times 1314 \times 18}{18 \times 18 \times 18} = 1183914$$

3.

(b) -11

**Explanation:**  $3x^2 + (k - 1)x + 9 = 0$

$x = 3$  is a solution of the equation means it satisfies the equation

Put  $x = 3$ , we get

$$3(3)^2 + (k - 1)3 + 9 = 0$$

$$27 + 3k - 3 + 9 = 0$$

$$27 + 3k + 6 = 0$$

$$3k = -33$$

$$k = -11$$

4.

(b)  $x^0 = 85^0$  and  $y^0 = 55^0$

**Explanation:** According to the question,

$$x^0 + y^0 + 40^0 = 180^0$$

$$x^0 + y^0 = 140^0 \dots (i)$$

$$\text{and } x^0 + y^0 = 30^0 \dots (ii)$$

$$\text{and } y^0 = 55^0$$

On solving eq. (i) and eq. (ii),

$$x + y + x - y = 140 + 30$$

$$2x = 170$$

$$x = 85^\circ$$

Putting the value of  $x$  in equation (i), we get

$$85^\circ + y = 140^\circ$$

$$y = 140^\circ - 85^\circ$$

$$y = 55^\circ$$

we get  $x^\circ = 85^\circ$  and  $y^\circ = 55^\circ$

5.

**(d) Real and Distinct roots**

**Explanation:** Comparing the given equation to the below equation

$$ax^2 + bx + c = 0$$

$$a = 1, b = -6, c = 6$$

$$D = b^2 - 4ac$$

$$D = (-6)^2 - 4 \times 1 \times 6$$

$$D = 36 - 24$$

$$D = 12$$

$$D > 0.$$

If  $b^2 - 4ac > 0$ , then the equation has real and distinct roots

Hence Real and Distinct roots.

6.

**(c) (-4, -15)**

**Explanation:** Let the vertex C be C (x,y). Then

$$\frac{-1+5+x}{1} = 0 \text{ and } \frac{4+2+y}{3} = -3 \Rightarrow x + 4 = 0 \text{ and } 6 + y = -9$$

$$\therefore x = -4 \text{ and } y = -15$$

so, the coordinates of C are (-4, -15).

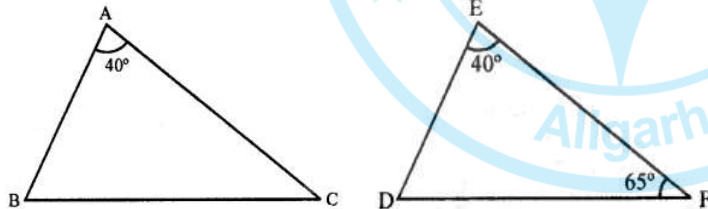
7.

**(a)  $75^\circ$**

**Explanation:** In  $\triangle ABC$  and  $\triangle DEF$

$$\angle A = \angle E = 40^\circ$$

$$AB : ED = AC : EF, \angle F = 65^\circ$$



$$\Rightarrow \frac{AB}{ED} = \frac{AC}{EF}$$

$\therefore$  In  $\triangle ABC$  and  $\triangle EDF$

$$\angle A = \angle E \quad (\text{each} = 40^\circ)$$

$$\frac{AB}{ED} = \frac{AC}{EF}$$

$\therefore \triangle ABC \sim \triangle EDF$  (SAS criterion)

$$\therefore \angle C = \angle F = 65^\circ$$

and  $\angle B = \angle D$

But  $\angle A + \angle B + \angle C = 180^\circ$  (Sum of angles of a triangle)

$$\Rightarrow 40^\circ + 65^\circ + \angle C = 180^\circ$$

$$\Rightarrow 105^\circ + \angle C = 180^\circ$$

$$\therefore \angle C = 180^\circ - 105^\circ = 75^\circ$$

8.

**(a) 13.5 cm.**

**Explanation:** In  $\triangle ABC$ ,

$$\Rightarrow \frac{AQ}{QC} = \frac{AP}{PB} \Rightarrow \frac{3}{6} = \frac{3.5}{7} \Rightarrow \frac{1}{2}$$

Since  $\frac{AQ}{QC} = \frac{AP}{PB}$ ,

therefore,  $QP \parallel BC$

$$\therefore \frac{AQ}{AC} = \frac{QP}{BC}$$

$$\Rightarrow \frac{1}{3} = \frac{4.5}{BC}$$

$$\Rightarrow BC = 13.5 \text{ cm}$$

9. (a) 6 cm

**Explanation:** Since the distance between two parallel tangents of a circle is equal to the diameter of the circle.

Given: Radius (OP) = 3 cm

$\therefore$  Diameter =  $2 \times$  Radius =  $2 \times 3 = 6$  cm

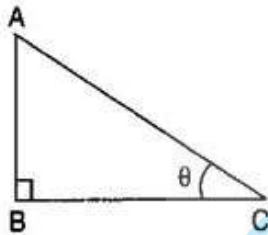
10.

(b)  $\frac{1-\cos \theta}{1+\cos \theta}$

$$\text{Explanation: } (\operatorname{cosec} \theta - \cot \theta)^2 = \left( \frac{1}{\sin \theta} - \frac{\cos \theta}{\sin \theta} \right)^2 = \frac{(1-\cos \theta)^2}{\sin^2 \theta} = \frac{(1-\cos \theta)^2}{(1-\cos^2 \theta)} = \frac{(1-\cos \theta)}{(1+\cos \theta)}$$

11.

(d)  $60^\circ$



**Explanation:**

Let AB be the electric pole of height  $10\sqrt{3}$  m and its shadow be BC of length 10 m. And the angle of elevation of the sun be  $\theta$ .

$$\therefore \tan \theta = \frac{AB}{BC}$$

$$\Rightarrow \tan \theta = \frac{10\sqrt{3}}{10}$$

$$\Rightarrow \tan \theta = \sqrt{3}$$

$$\Rightarrow \tan \theta = \tan 60^\circ$$

$$\Rightarrow \theta = 60^\circ$$

12.

(c)  $\frac{1-\cos \theta}{\sin \theta}$

$$\text{Explanation: We have, } \frac{\sin \theta}{1+\cos \theta} = \frac{\sin \theta(1-\cos \theta)}{(1+\cos \theta)(1-\cos \theta)}$$

$$= \frac{\sin \theta(1-\cos \theta)}{1-\cos^2 \theta} = \frac{\sin \theta(1-\cos \theta)}{\sin^2 \theta}$$

$$= \frac{1-\cos \theta}{\sin \theta}$$

13.

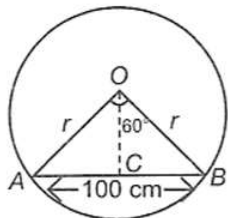
(a)  $\frac{\pi r^2 \theta}{360}$

$$\text{Explanation: } \frac{\pi r^2 \theta}{360}$$

14.

(c)  $30520.61 \text{ cm}^2$

**Explanation:** In  $\triangle OAB$ , by angle sum property



$$60^\circ + \angle OAB + \angle OBA = 180^\circ$$

$$\Rightarrow 2\angle OAB = 120^\circ \Rightarrow \angle OAB = 60^\circ$$

$\Rightarrow \triangle OAB$  is an equilateral triangle.

$$\Rightarrow r = 100 \text{ cm}$$

Area of major segment

$$= \text{Area of major sector} + \text{Area of } \triangle OAB$$

$$\begin{aligned}
 &= \frac{(360^\circ - 60^\circ)}{360^\circ} \times \pi r^2 + \frac{\sqrt{3}}{4} r^2 \\
 &= \frac{300}{360} \times \frac{22}{7} \times (100)^2 + \frac{\sqrt{3}}{4} \times 100^2 \\
 &= \frac{5}{6} \times \frac{22}{7} \times (100)^2 + \sqrt{3} \times 2500 \\
 &= 26190.48 + 4330.13 = 30520.61 \text{ cm}^2
 \end{aligned}$$

15. (a)  $\frac{5}{11}$

**Explanation:** Total number of fish = 15 + 18 = 33

Male fish = 15

Number of possible outcomes = 15

Number of total outcomes = 15 + 18 = 33

Required Probability =  $\frac{15}{33} = \frac{5}{11}$

16. (a) 0.5

**Explanation:** Given data = 30, 34, 35, 36, 37, 38, 39, 40

Here n = 8 which is even

$\therefore$  Median =  $\frac{1}{2} \left[ \left( \frac{n}{2} \right) \text{th} + \left( \frac{n}{2} + 1 \right) \text{th} \right]$  term =  $\frac{1}{2} (4\text{th} + 5\text{th term})$

=  $\frac{1}{2} (36 + 37) = \frac{73}{2} = 36.5$

After removing 35, then n = 7

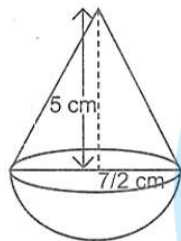
$\therefore$  New median =  $\frac{7+1}{2}$ th term = 4th term = 37

$\therefore$  Increase in median = 37 - 36.5 = 0.5

17.

(b) 616 cm<sup>3</sup>

**Explanation:**



Volume of water in the cylindrical tub = Volume of the tub

$$= \pi r^2 h = \left( \frac{22}{7} \times 5 \times 5 \times 9.8 \right) \text{ cm}^3 = 770 \text{ cm}^3$$

Volume of the solid immersed in the tub = Volume of the hemisphere + Volume of the cone

$$= \left[ \left( \frac{2}{3} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times \frac{7}{2} \right) + \left( \frac{1}{3} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 5 \right) \right] \text{ cm}^3$$

$$= \left( \frac{539}{6} + \frac{385}{6} \right) \text{ cm}^3 = \left( \frac{924}{6} \right) \text{ cm}^3 = 154 \text{ cm}^3$$

Volume of water left in the tub = Volume of the tub - Volume of solid immersed

$$= (770 - 154) \text{ cm}^3 = 616 \text{ cm}^3$$

18.

(d) 6

**Explanation:** Mean = 8.1

$$\sum f_i x_i = 132 + 5k$$

$$\sum f_i = 20$$

$$\therefore \text{Mean} = \frac{\sum f_i x_i}{\sum f_i} \Rightarrow 8.1 = \frac{132+5k}{20}$$

$$\Rightarrow 132 + 5k = 8.1 \times 20 = 162$$

$$\Rightarrow 5k = 162 - 132 = 30$$

$$\Rightarrow k = \frac{30}{5} = 6$$

19. (a) Both A and R are true and R is the correct explanation of A.

**Explanation:** Distance of point (5, 12) from 8 origin is given,  $d = \sqrt{(5-0)^2 + (12-0)^2}$

$$= \sqrt{25 + 144} = \sqrt{169} = 13$$

20. (a) Both A and R are true and R is the correct explanation of A.

**Explanation:** 380 is not divisible by 18.



**Section B**

21.  $2x - 2y - 2 = 0$ .....(1)

$4x - 4y - 5 = 0$ .....(2)

Here,  $a_1 = 2, b = -2, c_1 = -2$

$a_2 = 4, b_2 = -4, c_2 = -5$

We see that  $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$

Hence, the lines represented by the equations(1) and ( 2 ) are parallel.

Therefore, equations ( 1) and (2) have no solution, i.e., the given pair of a linear equation is inconsistent.

22. According to question it is given that D and E are the points on sides AB and AC respectively

Also  $AD = \frac{1}{3}BD$ ,

$AE = 4.5 \text{ cm}, DE \parallel BC$

$\therefore \frac{AD}{BD} = \frac{AE}{EC}$

$\Rightarrow \frac{\frac{1}{3}BD}{BD} = \frac{4.5}{EC}$

$\Rightarrow \frac{1}{3} = \frac{4.5}{EC}$

$\Rightarrow EC = 4.5 \times 3 \text{ cm}$

$\Rightarrow EC = 13.5 \text{ cm}$

Now,  $AC = AE + EC = 4.5 + 13.5 = 18 \text{ cm}$

OR

According to question it is given that ABCD is a rectangle and p is the midpoint of DC.

$\therefore AD = BC = 9 \text{ cm}$

$QC = BQ + BC = 7 + 9 = 16 \text{ cm}$

$PC = \frac{1}{2}CD \Rightarrow PC = 12 \text{ cm}$

In right  $\triangle PCQ$  using Pythagoras theorem

$PQ^2 = QC^2 + PC^2$

$PQ^2 = 16^2 + 12^2 = 400 \Rightarrow PQ = 20 \text{ cm}$

In right  $\triangle ABQ$  using Pythagoras theorem

$AQ^2 = AB^2 + BQ^2 \Rightarrow AQ^2 = 24^2 + 7^2 = 625$

$\Rightarrow AQ = 25 \text{ cm}$

In right  $\triangle ADP$  using Pythagoras theorem

$AP^2 = AD^2 + DP^2 \Rightarrow AP^2 = 9^2 + 12^2$

$\Rightarrow AP^2 = 81 + 144$

$\Rightarrow AP^2 = 225$

$AP = 15 \text{ cm}$

In  $\triangle APQ$ ,

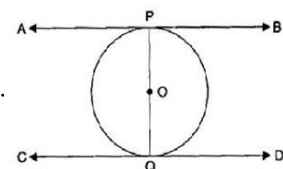
$AP^2 = 15^2 = 225$

$PQ^2 = 20^2 = 400 \Rightarrow AP^2 + PQ^2 = 625$

Also,  $AQ^2 = 25^2 = 625 \Rightarrow AQ^2 = AP^2 + PQ^2$

$\therefore \triangle APQ$  is a right angled  $\triangle$ (using converse of BPT)

$\therefore \angle APQ = 90^\circ$



23.

Given: PQ is a diameter of a circle with centre O.

The lines AB and CD are the tangents at P and Q respectively.

To Prove:  $AB \parallel CD$

Proof: Since AB is a tangent to the circle at P and OP is the radius through the point of contact.

$\therefore \angle OPA = 90^\circ$  ..... (i)

[The tangent at any point of a circle is  $\perp$  to the radius through the point of contact]

$\therefore$  CD is a tangent to the circle at Q and OQ is the radius through the point of contact.

$\therefore \angle OQD = 90^\circ$  ..... (ii)

[The tangent at any point of a circle is  $\perp$  to the radius through the point of contact]

From eq. (i) and (ii),  $\angle OPA = \angle OQD$

But these form a pair of equal alternate angles also,

$\therefore AB \parallel CD$

24. Given:

$$\operatorname{cosec}^2 \theta (1 + \cos \theta)(1 - \cos \theta) = \lambda$$

$$\Rightarrow \operatorname{cosec}^2 \theta \{(1 + \cos \theta)(1 - \cos \theta)\} = \lambda$$

$$\Rightarrow \operatorname{cosec}^2 \theta (1 - \cos^2 \theta) = \lambda$$

$$\Rightarrow \operatorname{cosec}^2 \theta \sin^2 \theta = \lambda$$

$$\Rightarrow \frac{1}{\sin^2 \theta} \times \sin^2 \theta = \lambda$$

$$\Rightarrow 1 = \lambda$$

$$\Rightarrow \lambda = 1$$

Thus, the value of  $\lambda$  is 1.

25. We have,  $r = 16.5$  km and  $\theta = 80^\circ$ .

Let A be the area of the sea over which the ships are warned. Then,

$$A = \frac{\theta}{360} \times \pi r^2 = \frac{80}{360} \times 3.14 \times 16.5 \times 16.5 \text{ km}^2 = 189.97 \text{ km}^2$$

OR

We have

$$R = 6 \text{ cm}$$

$$\text{Length of the arc} = 3\pi \text{ cm}$$

$$\text{as we know that arc length} = \frac{\theta}{360} \times 2\pi r$$

Substituting the values we get,

$$3\pi = \frac{\theta}{360} \times 2\pi \times 6 \dots (1)$$

Now we will simplify the equation (1) as below,

$$3\pi = \frac{\theta}{360} \times 12\pi$$

$$3\pi = \frac{\theta}{30} \times \pi$$

$$3 = \frac{\theta}{30}$$

$$\theta = 90^\circ$$

Therefore, the angle subtended at the centre of the circle is  $90^\circ$ .

Section C

26. Let us prove  $\sqrt{5}$  irrational by contradiction.

Let us suppose that  $\sqrt{5}$  is rational. It means that we have co-prime integers  $a$  and  $b$  ( $b \neq 0$ )

$$\text{Such that } \sqrt{5} = \frac{a}{b}$$

$$\Rightarrow b\sqrt{5} = a$$

Squaring both sides, we get

$$\Rightarrow 5b^2 = a^2 \dots (1)$$

It means that 5 is factor of  $a^2$

Hence, 5 is also factor of  $a$  by Theorem. ... (2)

If, 5 is factor of  $a$ , it means that we can write  $a = 5c$  for some integer  $c$ .

Substituting value of  $a$  in (1),

$$5b^2 = 25c^2$$

$$\Rightarrow b^2 = 5c^2$$

It means that 5 is factor of  $b^2$ .

Hence, 5 is also factor of  $b$  by Theorem. ... (3)

From (2) and (3), we can say that 5 is factor of both  $a$  and  $b$ .

But,  $a$  and  $b$  are co-prime.

Therefore, our assumption was wrong.  $\sqrt{5}$  cannot be rational. Hence, it is irrational.

27.  $\therefore \alpha$  and  $\beta$  are zeroes of given polynomial

$$\text{So, } x^2 + 9x + 20 = 0$$

$$x^2 + 4x + 5x + 20 = 0$$

$$x(x + 4) + 5(x + 4) = 0$$

$$(x + 5)(x + 4) = 0$$

$$x = -5 \text{ and } x = -4$$

$$\therefore \alpha = -5 \text{ and } \beta = -4$$

$$\text{Now, } \alpha + 1 = -4 \text{ and } \beta + 1 = -3$$

$$\text{So, product of zeroes} = (-4) \times (-3) = 12$$

$$\text{Sum of zeroes} = -7$$

$$\text{Now polynomial} = x^2 - (\text{sum of zeroes})x + (\text{product of zeroes})$$

$$\text{Polynomial} = x^2 + 7x + 12$$

28. The given equations are

$$\sqrt{2}x - \sqrt{3}y = 0 \dots\dots\dots(i)$$

$$\sqrt{3}x - \sqrt{8}y = 0 \dots\dots\dots(ii)$$

From equation (i), we obtain:

$$x = \frac{\sqrt{3}y}{\sqrt{2}} \dots\dots(iii)$$

Substituting this value in equation (ii), we obtain:

$$\sqrt{3} \left( \frac{\sqrt{3}y}{\sqrt{2}} \right) - \sqrt{8}y = 0$$

$$\frac{3y}{\sqrt{2}} - 2\sqrt{2}y = 0$$

$$y \left( \frac{3}{\sqrt{2}} - 2\sqrt{2} \right) = 0$$

$$y = 0$$

Substituting the value of y in equation (iii), we obtain:

$$x = 0$$

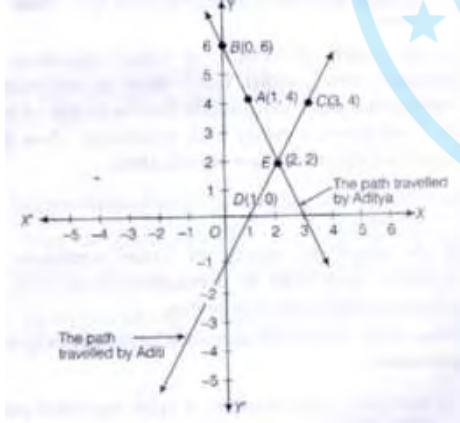
$$\therefore x = 0, y = 0$$

Hence the solution of given equation is (0,0).

OR

Let the given points be A(1,4), B(0,6), C(3,4) and D(1,0).

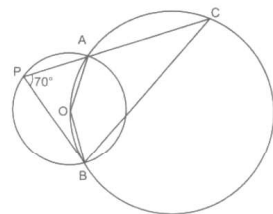
On plotting points A and B and joining them, we get the path travelled by Aditya. Similarly, on plotting points C and D and joining them, we get path travelled by Aditi.



It is clear from the graph that both of them cross each other at point E(2,2).

29. Consider the smaller circle whose centre is given as O.

The angle subtended by an arc at the centre of the circle is double the angle subtended by the arc in the remaining part of the circle.



Therefore, we have,

$$\angle AOB = 2\angle APB$$

$$= 2(70^\circ)$$

$$\angle AOB = 140^\circ$$

Now consider the larger circle and the points A, C, B and O along its circumference. AOBC from a cyclic quadrilateral.

In a cyclic quadrilateral, the opposite angles are supplementary, meaning that the opposite angles add up to  $180^\circ$ .

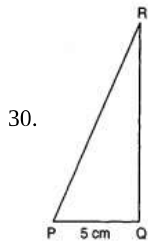
$$\angle AOB + \angle ACB = 180^\circ$$

$$\angle ACB = 180^\circ - \angle AOB$$

$$= 180^\circ - 140^\circ$$

$$\angle ACB = 40^\circ$$

Therefore, the measure of angle ACB is  $40^\circ$ .



In  $\triangle PQR$ , by Pythagoras theorem

$$PR^2 = PQ^2 + QR^2$$

$$\Rightarrow (25 - QR)^2 = 5^2 + QR^2 \quad [ \because PR + QR = 25 \text{ cm} \Rightarrow PR = 25 - QR ]$$

$$625 - 50QR + QR^2 = 25 + QR^2$$

$$\Rightarrow 600 - 50QR = 0$$

$$\Rightarrow QR = \frac{600}{50} = 12 \text{ cm}$$

$$\text{Now, } PR + QR = 25 \text{ cm}$$

$$\Rightarrow PR = 25 - QR = 25 - 12 = 13 \text{ cm}$$

$$\text{Hence, } \sin P = \frac{QR}{PR} = \frac{12}{13}, \cos P = \frac{PQ}{PR} = \frac{5}{13} \text{ and, } \tan P = \frac{QR}{PQ} = \frac{12}{5}$$

OR

$$\text{LHS} = \frac{\cos^3 \theta + \sin^3 \theta}{\cos \theta + \sin \theta} + \frac{\cos^3 \theta - \sin^3 \theta}{\cos \theta - \sin \theta}$$

$$= \frac{(\cos \theta + \sin \theta)(\cos^2 \theta + \sin^2 \theta - \sin \theta \cos \theta)}{(\cos \theta + \sin \theta)} + \frac{(\cos \theta - \sin \theta)(\cos^2 \theta + \sin^2 \theta + \sin \theta \cos \theta)}{(\cos \theta - \sin \theta)}$$

$$= (1 - \sin \theta \cos \theta) + (1 + \sin \theta \cos \theta)$$

$$= 1 + 1 - \sin \theta \cos \theta + \sin \theta \cos \theta$$

$$= 2 = \text{RHS}$$

31. Total number of cards in one deck of cards is 52.

$\therefore$  Total number of outcomes  $n = 52$

i. Let  $E_1$  = Event of getting a king of red color. So number of outcomes favourable to  $E_1$   $m = 2$  So  $P(E_1) = \frac{m}{n} = \frac{2}{52} = \frac{1}{26}$

ii. Let  $E_2$  = Event of getting a face card

$\therefore$  Numbers of outcomes favourable to  $E_2$ ,  $m = 12$ . Hence  $P(E_2) = \frac{m}{n} = \frac{12}{52} = \frac{3}{13}$

iii. Let  $E_3$  = Event of getting a red face card

$\therefore$  Numbers of outcomes favourable to  $E_3 = 6$  [  $\because$  there are 6 red face cards in a deck ] Hence  $P(E_3) = \frac{m}{n} = \frac{6}{52} = \frac{3}{26}$

iv. Let  $E_4$  = Event of getting a jack of heart

$\therefore$  Numbers of outcomes favourable to  $E_4 = 1$  [  $\because$  there is only one jack of heart in deck of cards.]

$$\text{Hence } P(E_4) = \frac{m}{n} = \frac{1}{52}$$

v. Let  $E_5$  = Event of getting a spade

$\therefore$  Numbers of outcomes favourable to  $E_5 = 13$  [  $\because$  there are 13 spade in a deck ]

$$\text{Hence } P(E_5) = \frac{m}{n} = \frac{13}{52}$$



vi. Let  $E_6$  = Event of getting the queen of diamond

$\therefore$  Numbers of outcomes favourable to  $E_6 = 1$  [  $\therefore$  there is only one queen of diamond in a deck]

Hence,  $P(E_6) = \frac{m}{n} = \frac{1}{52}$

**Section D**

32. We have given,

$$\left(\frac{2x}{x-5}\right)^2 + 5\left(\frac{2x}{x-5}\right) - 24 = 0$$

Let  $\frac{2x}{x-5}$  be  $y$

$$\therefore y^2 + 5y - 24 = 0$$

Now factorise,

$$y^2 + 8y - 3y - 24 = 0$$

$$y(y + 8) - 3(y + 8) = 0$$

$$(y + 8)(y - 3) = 0$$

$$y = 3, -8$$

Putting  $y = 3$

$$\frac{2x}{x-5} = 3$$

$$2x = 3x - 15$$

$$x = 15$$

Putting  $y = -8$

$$\frac{2x}{x-5} = -8$$

$$2x = -8x + 40$$

$$10x = 40$$

$$x = 4$$

Hence,  $x$  is 15, 4

OR

According to the question, let the consecutive multiples of 7 be  $7x$  and  $7x + 7$

$$(7x)^2 + (7x + 7)^2 = 637$$

$$\text{or, } 49x^2 + 49x^2 + 49 + 98x = 637$$

$$\text{or, } 98x^2 + 98x - 588 = 0$$

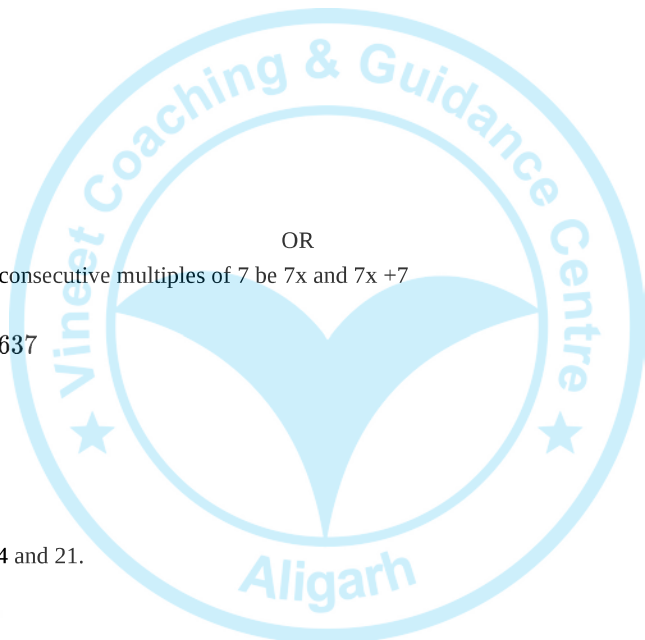
$$\text{or, } x^2 + x - 6 = 0$$

$$\text{or, } (x + 3)(x - 2) = 0$$

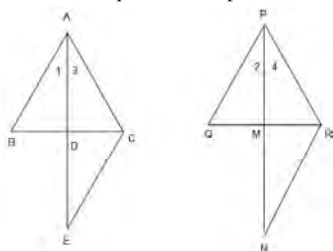
$$\text{or, } x = -3, 2$$

Rejecting the value,  $x = 2$

Thus, the required multiples are, 14 and 21.



33.



Given : In  $\triangle ABC$  and  $\triangle PQR$  The  $AD$  and  $PM$  are their medians,

such that  $\frac{AB}{PQ} = \frac{AD}{PM} = \frac{AC}{PR}$

To prove :  $\triangle ABC \sim \triangle PQR$

Construction : Produce  $AD$  to  $E$  such that  $AD = DE$  and produce  $PM$  to  $N$  such that  $PM = MN$ . Join  $CE$  and  $RN$ .

Proof : In  $\triangle ABD$  and  $\triangle EDC$

$$AD = DE$$

$$\angle ADB = \angle EDC \text{ (vertically opposite angles)}$$

$$BD = DC \text{ (as } AD \text{ is a median)}$$

$$\therefore \triangle ABD \cong \triangle EDC \text{ (By SAS congruency)}$$

$$\text{or, } AB = CE \text{ (By CPCT)}$$

Similarly,  $PQ = RN$

$$\frac{AB}{PQ} = \frac{AD}{PM} = \frac{AC}{PR} \text{ (Given)}$$

$$\text{or, } \frac{CE}{RN} = \frac{2AD}{2PM} = \frac{AC}{PR}$$

$$\text{or } \frac{CE}{RN} = \frac{AE}{PN} = \frac{AC}{PR}$$

So  $\triangle ACE \sim \triangle PRN$

$$\angle 3 = \angle 4$$

Similarly  $\angle 1 = \angle 2$

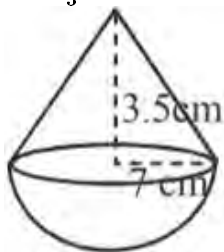
$$\angle 1 + \angle 3 = \angle 2 + \angle 4$$

So  $\angle A = \angle P$  and

$$\frac{AB}{PQ} = \frac{AC}{PR} \text{ (given)}$$

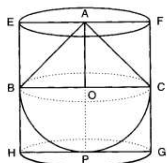
Hence  $\triangle ABC \sim \triangle PQR$

$$\begin{aligned} 34. \text{ Volume of solid} &= \frac{1}{3} \times \frac{22}{7} \times (7)^2 \times 3.5 + \frac{2}{3} \times \frac{22}{7} \times (7)^3 \\ &= \frac{22}{7} \times (7)^2 \times \left[ \frac{3.5}{3} + \frac{2}{3} \times 7 \right] \\ &= 898\frac{1}{3} \text{ or } 898.33 \text{ cm}^3 \end{aligned}$$



OR

Let BPC be the hemisphere and ABC be the cone mounted on the base of the hemisphere. Let EFGH be the right circular cylinder circumscribing the given toy.



We have,

$$\text{Given radius of cone, cylinder and hemisphere (r)} = \frac{4}{2} = 2 \text{ cm}$$

$$\text{Height of cone (l)} = 2 \text{ cm}$$

$$\text{Height of cylinder (h)} = 4 \text{ cm}$$

$$\text{Now, Volume of the right circular cylinder} = \pi r^2 h = \pi \times 2^2 \times 4 \text{ cm}^3 = 16\pi \text{ cm}^3$$

$$\text{Volume of the solid toy} = \left\{ \frac{2}{3}\pi \times 2^3 + \frac{1}{3}\pi \times 2^2 \times 2 \right\} \text{ cm}^3 = 8\pi \text{ cm}^3$$

$$\therefore \text{ Required space} = \text{Volume of the right circular cylinder} - \text{Volume of the toy}$$

$$= 16\pi \text{ cm}^3 - 8\pi \text{ cm}^3 = 8\pi \text{ cm}^3.$$

Hence, the right circular cylinder covers  $8\pi \text{ cm}^3$  more space than the solid toy.

$$\text{So, remaining volume of cylinder when toy is inserted in it} = 8\pi \text{ cm}^3$$

35. We may observe from the given data that maximum class frequency is 40 belonging to 1500 - 2000 interval.

$$\text{Class size (h)} = 500$$

$$\text{Mode} = l + \frac{f - f_1}{2f - f_1 - f_2} \times h$$

$$\text{Lower limit (l) of modal class} = 1500$$

$$\text{Frequency (f) of modal class} = 40$$

$$\text{Frequency (f}_1\text{) of class preceding modal class} = 24$$

$$\text{Frequency (f}_2\text{) of class succeeding modal class} = 33$$

$$\text{mode} = 1500 + \frac{40 - 24}{2 \times 40 - 24 - 33} \times 500$$

$$= 1500 + \frac{16}{80 - 57} \times 500$$

$$= 1500 + 347.826$$

$$= 1847.826 \approx 1847.83$$

Expenditure (in ₹.)	Number of families $f_i$	$x_i$	$d_i = x_i - 2750$	$u_i$	$u_i f_i$
1000-1500	24	1250	-1500	-3	-72
1500-2000	40	1750	-1000	-2	-80
2000-2500	33	2250	-500	-1	-33
2500-3000	28	2750=a	0	0	0
3000-3500	30	3250	500	1	30
3500-4000	22	3750	1000	2	44
4000-4500	16	4250	1500	3	48
4500-5000	7	4750	2000	4	28
	$\Sigma f_i = 200$				$\Sigma f_i d_i = -35$

$$\text{Mean } \bar{x} = a + \frac{\Sigma f_i d_i}{\Sigma f_i} \times h$$

$$\bar{x} = 2750 + \frac{-35}{200} \times 500$$

$$\bar{x} = 2750 - 87.5$$

$$\bar{x} = 2662.5$$

### Section E

36. i. The number of rose plants in the 1<sup>st</sup>, 2<sup>nd</sup>, .... are 23, 21, 19, ... 5

$$a = 23, d = 21 - 23 = -2, a_n = 5$$

$$\therefore a_n = a + (n - 1)d$$

$$\text{or, } 5 = 23 + (n - 1)(-2)$$

$$\text{or, } 5 = 23 - 2n + 2$$

$$\text{or, } 5 = 25 - 2n$$

$$\text{or, } 2n = 20$$

$$\text{or, } n = 10$$

- ii. Total number of rose plants in the flower bed,

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$S_{10} = \frac{10}{2} [2(23) + (10 - 1)(-2)]$$

$$S_{10} = 5[46 - 20 + 2]$$

$$S_{10} = 5(46 - 18)$$

$$S_{10} = 5(28)$$

$$S_{10} = 140$$

- iii.  $a_n = a + (n - 1)d$

$$\Rightarrow a_6 = 23 + 5 \times (-2)$$

$$\Rightarrow a_6 = 13$$

**OR**

$$S_n = 80$$

$$S_n = \frac{n}{2} [2a + (n - 1)d]$$

$$\Rightarrow 80 = \frac{n}{2} [2 \times 23 + (n - 1) \times (-2)]$$

$$\Rightarrow 80 = 23n - n^2 + n$$

$$\Rightarrow n^2 - 24n + 80 = 0$$

$$\Rightarrow (n - 4)(n - 20) = 0$$

$$\Rightarrow n = 4 \text{ or } n = 20$$

$n = 20$  not possible

$$a_{20} = 23 + 19 \times (-2) = -15$$

Number of plants cannot be negative.

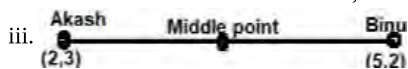
$$n = 4$$

37. i. Position of Neena = (3, 6)

Position of Karan = (6, 5)

$$\begin{aligned} \text{Distance between Neena and Karan} &= \sqrt{(6-3)^2 + (5-6)^2} \\ &= \sqrt{9 + (-1)^2} \\ &= \sqrt{10} \end{aligned}$$

ii. Co-ordinate of seat of Akash = 2, 3



$$\text{Co-ordinate of middle point} = \left( \frac{2+5}{2}, \frac{3+2}{2} \right)$$

$$= 3.5, 2.5$$

**OR**

Binu = (5, 5); Karan = (6, 5)

$$\text{Distance} = \sqrt{(6-5)^2 + (5-2)^2}$$

$$= \sqrt{1+9}$$

$$= \sqrt{10}$$

38. Let h is height of big building, here as per the diagram.

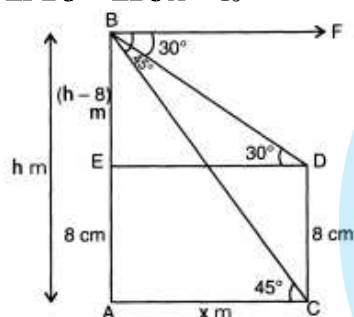
AE = CD = 8 m (Given)

BE = AB - AE = (h - 8) m

Let AC = DE = x

Also,  $\angle FBD = \angle BDE = 30^\circ$

$\angle FBC = \angle BCA = 45^\circ$



In  $\triangle ACB$ ,  $\angle A = 90^\circ$

$$\tan 45^\circ = \frac{AB}{AC}$$

$$\Rightarrow x = h, \dots(i)$$

In  $\triangle BDE$ ,  $\angle E = 90^\circ$

$$\tan 30^\circ = \frac{BE}{ED}$$

$$\Rightarrow x = \sqrt{3}(h - 8) \dots(ii)$$

From (i) and (ii), we get

$$h = \sqrt{3}h - 8\sqrt{3}$$

$$h(\sqrt{3} - 1) = 8\sqrt{3}$$

$$h = \frac{8\sqrt{3}}{\sqrt{3}-1} = \frac{8\sqrt{3}}{\sqrt{3}-1} \times \frac{\sqrt{3}+1}{\sqrt{3}+1}$$

$$= \frac{1}{2} \times (24 + 8\sqrt{3}) = \frac{1}{2} \times (24 + 13.84) = 18.92m$$

Hence height of the multistory building is 18.92 m and the distance between two buildings is 18.92 m.

